# MATHEMATICS

Our Website (http://www.math.vt.edu)

# **Overview**

Mathematics is essential to a clear and complete understanding of virtually all phenomena. Its precision, depth, and generality support the development of critical thinking and problem-solving skills. The study of mathematics provides the ability to describe applied problems quantitatively and to analyze these problems in a precise and logical manner. This is a principal reason behind the strong demand for mathematicians in government and industry. Essentially all complex problems, whether physical, social, or economic, are solved by designing a mathematical model, analyzing the model, and determining computational algorithms for an efficient and accurate approximation of a solution. Each of these phases is mathematical in nature. For example, if a problem deviates from a standard form, a mathematician should be able to adjust the usual mathematical treatment of the problem to accommodate the deviation. In this case mathematical training provides a practical preparation for a career in today's changing world. Moreover, it is especially valuable because it is an education that equips one to continue to adapt to new situations.

Mathematicians typically are employed as applied mathematicians in their specialty areas. Our recent mathematics graduates have been divided among government and industry, graduate school, and teaching. There are four different paths or degree options that a student may follow towards a B.S. in Mathematics:

- 1. the Traditional Option;
- 2. the Applied Computational Mathematics Option (ACM);
- 3. the Applied Discrete Mathematics Option (ADM); and
- 4. the Mathematics Education Option (MSTR).

The Traditional Option, as its name implies, yields a broad and flexible background in mathematics, while the other three options are more specialized. The ACM option is designed for students who want to have an applied mathematics career in an area closely associated with physics, some form of engineering, etc. The Traditional and ACM options require students to work with their advisor to create a plan of study for an Interdisciplinary Application of Mathematics. This plan consists of courses in an applied area of the student's choosing that will support their post-graduation goals. The ADM option is designed for students primarily interested in areas of applied mathematics closely associated with computer science. The Mathematics Education Option is designed for students who want to be certified to teach secondary mathematics.

The ADM Option is designed for students who want to have an applied mathematics career in an area closely associated with computer science. The Education Option is designed for students who want to teach high-school or middle-school mathematics. The ADM and Math Ed options have the Interdisciplinary Application of Mathematics and associated required courses already determined – computer science courses for ADM and teaching-focused courses for Math Ed. More details and specific requirements can be found in the Program Curriculum of each degree option.

Though each of the degree options has different graduation requirements, and each is intended to support various post-graduation goals, all four degree options yield the same degree – a B.S. in Mathematics. The first two years of coursework are nearly identical among the degree options, making it easy to change degree options early in your undergraduate mathematical career. It is critical that you discuss your mathematical interests and post-graduation goals with your advisor early and often in order to determine the degree option that will be best suited for you. If you are interested in graduate study, seek advice early and often about the degree option, coursework, and research experience(s) that provide the best preparation for graduate work in your mathematical area of interest.

# **Scholarships**

In a typical year the Math Department awards more than \$60,000 to 30+ students with the majority going to continuing students. Undergraduate students will be emailed with specific steps to follow in order to be considered for a Math Department awarded scholarship.

## Mathematical Contests, Competitions, and Activities

The Mathematics Department firmly believes that mathematics is not only useful and beautiful, but also fun. The department sponsors student chapters of MAA (Mathematical Association of America), SIAM (Society for Industrial and Applied Mathematics), Pi Mu Epsilon (the national mathematics honorary society), and AWM (Association for Women in Mathematics). As well as social activities, these groups sponsor speakers to talk on how mathematics is used in their work. Each fall, Virginia Tech also sponsors the Virginia Tech Regional Mathematics Contest. In addition, students (not all of whom are mathematics majors) may receive organized preparation and compete in the nationwide William Lowell Putnam Competition and the international Mathematical Contest in Modeling. Matecharlas provides students with the opportunity for informal discussions about 1000-level MATH courses with instructors fluent in Spanish. More information about these student chapters and activities can be found on our undergraduate website in the section titled Opportunities for VT Math Students: math.vt.edu/undergrad-math (https://math.vt.edu/undergrad-math.html)

## **Undergraduate Research**

The Mathematics Department at Virginia Tech emphasizes and features activity in undergraduate research. Numerous institutions, including the National Science Foundation, the American Mathematical Society, and the Society for Industrial & Applied Mathematics, also emphasize the importance of developing research opportunities for undergraduates. Undergraduate research experiences serve to prepare students for life after the B.S. degree, both in the industrial world and in graduate school.

There are several ways to participate in mathematics undergraduate research. Some students participate in projects with stipend support, some earn course credit as MATH 4994, and others participate purely for the experience. Undergraduate research projects are typically directed by faculty members. The Mathematics Department hosts a competition each spring, where undergraduates can present their research and the top presenter wins the Layman Prize. To find an undergrad research project to participate in, students are encouraged to reach out to any faculty member about potential research interests and/or to reach out to our faculty members who serve as the coordinators of our undergraduate research program. More information, including contact information for the Math Department Undergraduate Research Coordinators, research competitions and prizes, forms, and more can be found at: https://math.vt.edu/undergrad-math/undergraduate-research.html.

## **Honors Sections of Math Courses**

Several academic departments in the College of Science, including the Mathematics Department, offer special Honors sections of their courses. More information is available at math.vt.edu/honors (http://www.math.vt.edu/honors/). In addition to special sections of some courses, the Honors Office sponsors a colloquia series each semester. The colloquia explore special topics not in the University Curriculum. Details about the Honors College can be found at http:// www.honorscollege.vt.edu.

# Math Credit from College-Level Exams

Students can earn credit for math courses through college-level exams such as AP, IB, CLEP, Cambridge, etc. The most common credit earned through college-level exams is MATH 1225 Calculus of a Single Variable and possibly also MATH 1226 Calculus of a Single Variable. More information can be found at: https://www.registrar.vt.edu/Transferable-Credit.html

# **Senior Awards**

In each of the four degree options, one student is selected each year as the Outstanding Senior. An overall Outstanding Senior is also selected. All awardees are recognized at an awards reception in the spring semester. The College of Science has awards for one Outstanding Senior and one Outstanding Researcher among all students in the college, and the Math Department puts forward a nominee for each of these awards.

# Accelerated Undergraduate/Graduate Degree Program in Mathematics

The Accelerated Undergraduate/Graduate Degree Program is intended to allow undergraduate students who are prepared to take graduate courses to complete M.S. requirements one year after completing B.S. requirements.. The principal feature of the program is that it allows the students to use 12 credits of graduate work simultaneously toward the completion of their bachelor's degree and a program of study leading to a master's degree. It is this ability to complete the final year of undergraduate work with the same courses that comprise much of the first year of graduate work that makes it possible to finish both degrees in five years. For more information, students should contact the Math Department Graduate Program Director and consult: https:// www.math.vt.edu/content/dam/math\_vt\_edu/documents/accel-u-gdegree.pdf

Students in the Math Education degree option may apply to an optional fifth year to earn an M.A.Ed. in Curriculum & Instruction with a specialization in Mathematics Education in the Virginia Tech School of Education. The 5-year program is designed to satisfy Virginia's licensure requirements for teaching mathematics in secondary schools.

The department also offers a Ph.D. program.

# **Advising and Resources**

Math Department academic advisors are also faculty members who can discuss details of course and career advice throughout your undergraduate career, in addition to many other aspects of undergraduate educational life. Advising information and resources can be found at: math.vt.edu/advising (https://math.vt.edu/undergrad-math/ advising.html).

In addition to your assigned academic advisor, the Mathematics Department has designated Career Advisors. The Career Advisors will work with your academic advisor to provide information that will aid you in planning a career-oriented program. Information about career opportunities and career fairs will be sent to students periodically. In addition, you can explore the career resources and information posted on the Math Department's Career Advising website: math.vt.edu/careers (http://www.math.vt.edu/careers/).

Further information on the Mathematics Program can be found at www.math.vt.edu (http://www.math.vt.edu).

# **Minor in Mathematics**

### Requirements

At least 26 credits comprised of: MATH 1225 Calculus of a Single Variable, MATH 1226 Calculus of a Single Variable, MATH 2204 Introduction to Multivariable Calculus, MATH 2114 Introduction to Linear Algebra, MATH 2214 Introduction to Differential Equations and 9 hours of approved mathematics courses numbered 3000 or higher. See Math Minor requirements for details, exceptions, and allowed substitutions. Students are required to have 2.0 in-minor GPA and all courses used for the math minor must be taken in A-F grade mode. To graduate with a Virginia Tech undergraduate degree, a minimum of 25% of total credits for majors and minors must be taken at Virginia Tech. This means at least 7 credits for the math minor must be taken at Virginia Tech.

- Mathematics Major (https://catalog.vt.edu/undergraduate/collegescience/mathematics/mathematics-bs/)
- Mathematics Major with Applied Computational Mathematics Option (https://catalog.vt.edu/undergraduate/college-science/mathematics/ mathematics-bs-applied-computational-mathematics/)
- Mathematics Major with Applied Discrete Mathematics Option (https://catalog.vt.edu/undergraduate/college-science/mathematics/ mathematics-bs-applied-discrete-mathematics/)
- Mathematics Major with Mathematics Education (Master's Track) Option (https://catalog.vt.edu/undergraduate/college-science/ mathematics/mathematics-bs-mathematics-education-masterstrack/)

#### Chair: Sarah Reznikoff

Director for Undergraduate Programs: N. Loehr Graduate Director: A. Norton Class of 1950 Professor in Mathematics: S. Gugercin John K. Costain Faculty Chair and Professor. T. Warburton Hatcher Professor of Mathematics: J. A. Burns Professors: S. Adjerid, D. Appelo, C. A. Beattie, J. Borggaard, Y. Cheng, S. Ciupe, E. de Sturler, A. Elgart, M. Embree, P. E. Haskell, T. L. Herdman, T. Iliescu, T. Lin, N. Loehr, G. Matthews, A. Miedlar, C. Mihalcea, A. Norton, M. Shimozono, S. Sun, S. T. Warburton, M. Wawro, and P. Yue Associate Professors: N. Abaid, L. Childs, H. Liu, D. Orr, E. Palsson, P. Wapperom, P. Yue, and L. Zietsman Assistant Professors: G. Camliyurt, P. Cazeaux, A. Deuchert, D. Douglas, I. Fracas, E. Johnson, J. LeGrow, H. Leo, H. Lopez Valdez, J. Madrid Padilla, E. Martin, T. Morrison, M. Pasha, M. Robert, J. Rudi, A. Sarah, O. Saucedo, W. Sun, S. Werner, and Y. Yang Collegiate Associate Professors: R. Arnold Collegiate Assistant Professors: E. Ufferman and J. Wilson Visiting Assistant Professors: G. Alam, A. Biswas, K. Flanagan, P. Manoharan, S. Pantic, K. Saglam, and R. Steiner, and T. Topcu Patricia Ann Caldwell Post-Doctoral Fellow and Visiting Assistant Professor: I. Huq-Kuruvilla and R. Singh Senior Instructors: D. Agud, T. A. Bourdon, J. Clemons, H. Hart, J. Hurdus, N. Robbins, and J. Schmale.

Advanced Instructors: S. Barreto, M. Chung, S. Hammer, E. Jasso Hernandez, K. Karcher, C. Letona, M. Ouliaei-Nia, S. Silber, J. Thompson, and K. Zachrich Instructors: H. Abobaker, T. Asfaw, S. Aslan, T. Balkew, J. Burleson, D. Callie, R. Carracedo Rodriguez, P. Caruso, S. Cvitanov, F. Elsrrawi, J. England, J. Evans, H. Farhat, G. Fowler, N. Garcia Hilares, P. Jones, T. Juste, K. Kasebian, D. Kim, M. Mahmood, N. Malik, B. Nguyen, C. Nicolas, K. Perera, S. Pidaparthi, I. Quinlan, E. F. Rabby, K. Robinson, Rappold, G. Seebohm, R. Sharpe, J. St.Clair, J. Truman, D. Valvo, J. Wells, and C. Withrow

#### Presidential Postdoctoral Associate: E. Camps Moreno

**Postdoctoral Associates:** J. Antonides, E. Camps, K. Castellano, L. LeJeune, H. Jiuhua, P. Mlimarć, J. Reyes, W. Santos, P. Soto, P. Tsai, and F. Yan

#### Senior Research Associate: S. Meng

Lecturers: V. Kairamkonda, W. Reilly, A. Sibol, and E. Widdowson Career Advisors: E. de Sturler and J. Wilson Scholarship Chair: L. Childs

# Undergraduate Course Descriptions (MATH)

#### MATH 1004 - Discovering Mathematics I (1 credit)

Introduction to the scope and applicability of mathematics and its many sub-disciplines. Introduction to the process of thinking, learning, and writing as a mathematician through topics such as logic systems, recreational mathematics, LaTeX programming, history, ethics, open problems, and research in mathematics. Also includes advising topics such as planning a Virginia Tech course of study. P/F only. Math majors. Instructional Contact Hours: (1 Lec, 1 Crd)

#### MATH 1014 - Precalculus with Transcendental Functions (3 credits)

Precalculus college algebra, basic functions (algebraic, exponential, logarithmic, and trigonometric), conic sections, graphing techniques, basic probability. Usage of mathematical models, analytical calculations, and graphical or numerical representations of data to analyze problems from multiple disciplines that address intercultural and global challenges in areas such as chemistry, environmental science, the life sciences, finance, and statistics. Use of spreadsheet software. Two units of high school algebra and one of plane geometry are required. **Pathway Concept Area(s):** 5F Quant & Comp Thnk Found., 11

Intercultural&Global Aware.

Instructional Contact Hours: (3 Lec, 3 Crd)

# MATH 1025 - Elementary Calculus (3 credits)

Quantitative and computational thinking to address relevant global issues. Unified calculus course covering techniques and applications of differential and integral calculus for functions of one variable. Constitutes the standard first-year mathematics courses for the life sciences. 1025: Differential calculus, graphing, applications for the life sciences, use of spreadsheet software. Assumes 2 units of high school algebra, 1 unit of geometry, 1/2 unit of trigonometry and precalculus. 1026: Integral calculus, numerical techniques, elementary differential equations, applications for the life sciences, use of spreadsheet and scientific software. A student can earn credit for at most one of 1025 and 1225. A student can earn credit for at most one of 1026 and 1226. **Pathway Concept Area(s):** 5F Quant & Comp Thnk Found., 11 Intercultural&Global Aware.

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 1026 - Elementary Calculus (3 credits)

Quantitative and computational thinking to address relevant global issues. Unified calculus course covering techniques and applications of differential and integral calculus for functions of one variable. Constitutes the standard first-year mathematics courses for the life sciences. 1025: Differential calculus, graphing, applications for the life sciences, use of spreadsheet software. Assumes 2 units of high school algebra, 1 unit of geometry, 1/2 unit of trigonometry and precalculus. 1026: Integral calculus, numerical techniques, elementary differential equations, applications for the life sciences, use of spreadsheet and scientific software. A student can earn credit for at most one of 1025 and 1225. A student can earn credit for at most one of 1026 and 1226. **Prereguisite(s):** MATH 1025 or MATH 1225

Pathway Concept Area(s): 5F Quant & Comp Thnk Found., 11

Intercultural&Global Aware.

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 1044 - Discovering Mathematics II (2 credits)

Introduction to the scope and applicability of mathematics and its many sub-disciplines. Introduction to the process of thinking, learning, and writing as a mathematician through topics in pure and applied mathematics and a brief experience with mathematical research. Also includes advising topics such as planning a Virginia Tech course of study. Math majors.

Instructional Contact Hours: (2 Lec, 2 Crd)

#### MATH 1214 - Preparation for Calculus (3 credits)

Linear equations, polynomials, relations and functions, rational functions, quadratic equations, radicals and functions with rational exponents, exponentials, logarithms, trigonometric functions, trigonometric identities. Designed as preparation for MATH 1225: Calculus of a Single Variable.

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 1225 - Calculus of a Single Variable (4 credits)

1225-1226: CALCULUS OF A SINGLE VARIABLE Quantitative and computational thinking to address relevant intercultural and global issues. Unified calculus course covering techniques of differential and integral calculus for functions of one variable. Constitutes the standard first-year mathematics courses for science and engineering. 1225: limits, continuity, differentiation, transcendental functions, applications of differentiation, introduction to integration. Assumes 2 units of high school algebra, 1 unit of geometry, 1/2 unit each of trigonometry and precalculus, and placement by Math Dept. 1226: techniques and applications of integration, trapezoidal and Simpson's rules, improper integrals, sequences and series, power series, parametric curves and polar coordinates, software-based techniques. A student can earn credit for at most one of 1025 and 1225. A student can earn credit for at most one of 1525 and 1225. A student can earn credit for at most one of 1026 and 1226. Pre: Grade of at least C- in 1225 for 1226.

Prerequisite(s): MATH 1214

Pathway Concept Area(s): 5F Quant & Comp Thnk Found., 11 Intercultural&Global Aware.

Instructional Contact Hours: (4 Lec, 4 Crd)

#### MATH 1226 - Calculus of a Single Variable (4 credits)

1225-1226: CALCULUS OF A SINGLE VARIABLE Quantitative and computational thinking to address relevant intercultural and global issues. Unified calculus course covering techniques of differential and integral calculus for functions of one variable. Constitutes the standard first-year mathematics courses for science and engineering. 1225: limits, continuity, differentiation, transcendental functions, applications of differentiation, introduction to integration. Assumes 2 units of high school algebra, 1 unit of geometry, 1/2 unit each of trigonometry and precalculus, and placement by Math Dept. 1226: techniques and applications of integration, trapezoidal and Simpson's rules, improper integrals, sequences and series, power series, parametric curves and polar coordinates, software-based techniques. A student can earn credit for at most one of 1025 and 1225. A student can earn credit for at most one of 1525 and 1225. A student can earn credit for at most one of 1026 and 1226. Pre: Grade of at least C- in 1225 for 1226.

Prerequisite(s): MATH 1225

Pathway Concept Area(s): 5F Quant & Comp Thnk Found., 11 Intercultural&Global Aware.

Instructional Contact Hours: (4 Lec, 4 Crd)

#### MATH 1454 - Introduction to Programming for Mathematical Problem-Solving (3 credits)

Introduction to programming for mathematical problem solving. Programming software interfaces. Logic and conditional computations. Iterative computations and recursion. Data arrays. Compartmentalized computations using functions. Data visualization. Data input/output. Programming applications such as Monte Carlo simulation, random walks, computational geometry, and graph theory. Corequisite(s): MATH 1225

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 1524 - Business Calculus (4 credits)

Differential calculus techniques for functions of one and two variables. Emphasis on graphs, rates of change, and optimization of linear, guadratic, exponential, and logistic functions. Terminology and applications for business, including spreadsheet software. Mathematical models of real-world business problems, including discrete and continuous models, that address intercultural and global challenges in such areas as finance, marketing, and accounting. Assumes 2 units of high school algebra and 1 unit of geometry.

Pathway Concept Area(s): 5F Quant & Comp Thnk Found., 11 Intercultural&Global Aware.

Instructional Contact Hours: (4 Lec, 4 Crd)

#### MATH 1535 - Geometry and Mathematics of Design (3 credits)

A standard first-year mathematics sequence for architecture majors. Mathematical models of real-world problems, including discrete and continuous models, that address relevant global challenges in such areas as urban planning, building construction, and home design. 1535: Euclidean geometry, trigonometry, sequences and the golden ratio, graph theory, tilings, polygons and polyhedra, applications for 2- and 3dimensional design and construction, use of geometric software. 1536: vectors in the plane and space, descriptive and projective geometry, differential and integral calculus, applications for 2- and 3-dimensional design and construction, including areas, volumes, centroids, and optimization. Assumes 2 unites of high school algebra and 1 unit of high school geometry.

Pathway Concept Area(s): 5F Quant & Comp Thnk Found., 11 Intercultural&Global Aware.

#### Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 1536 - Geometry and Mathematics of Design (3 credits)

A standard first-year mathematics sequence for architecture majors. Mathematical models of real-world problems, including discrete and continuous models, that address relevant global challenges in such areas as urban planning, building construction, and home design. 1535: Euclidean geometry, trigonometry, sequences and the golden ratio, graph theory, tilings, polygons and polyhedra, applications for 2- and 3dimensional design and construction, use of geometric software. 1536: vectors in the plane and space, descriptive and projective geometry, differential and integral calculus, applications for 2- and 3-dimensional design and construction, including areas, volumes, centroids, and optimization. Assumes 2 unites of high school algebra and 1 unit of high school geometry.

Pathway Concept Area(s): 5F Quant & Comp Thnk Found., 11 Intercultural&Global Aware.

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 1614 - Numbers and Operations for Teachers (3 credits)

Study of the nature and structure of numbers for prospective elementary and middle school teachers; number theory, number systems, operations and algebraic thinking, problem solving, and mathematical modeling. 1614 may not be taken by math majors for credit. Instructional Contact Hours: (3 Lec, 3 Crd)

MATH 1624 - Geometry for Teachers (3 credits)

Study of key geometry concepts for prospective elementary and middle school teachers; multiple perspectives including transformational, coordinate, Euclidean and analytical geometry; geometric modeling; geometric and spatial reasoning. 1624 may not be taken by math majors for credit.

Prerequisite(s): MATH 1614

Instructional Contact Hours: (3 Lec, 3 Crd) MATH 1984 - Special Study (1-19 credits)

Instructional Contact Hours: Variable credit course

#### MATH 1984E - Special Study (3 credits)

Pathway Concept Area(s): 5F Quant & Comp Thnk Found. Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 2114 - Introduction to Linear Algebra (3 credits)

Vector and matrix algebra systems of linear equations, linear equations, linear independence, bases, orthonormal bases, rank, linear transformations, diagonalization, implementation with contemporary software. Math 1226 or a grade of at least B in VT MATH 1225. A student can earn credit for at most one of 2114 and 2405H.

Prerequisite(s): MATH 1225 or MATH 1226 Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 2114H - Introduction to Linear Algebra (3 credits)

Vector and matrix algebra systems of linear equations, linear equations, linear independence, bases, orthonormal bases, rank, linear transformations, diagonalization, implementation with contemporary software. Math 1226 or a grade of at least B in VT MATH 1225. A student can earn credit for at most one of 2114H and 2405H. Prerequisite(s): MATH 1225 or MATH 1226 or

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 2204 - Introduction to Multivariable Calculus (3 credits)

Calculus for functions for several variables. Planes and surfaces, continuity, differentiation, chain rule, extreme values, Lagrange multipliers, double and triple integrals and applications, software-based techniques. A student can earn credit for at most one of 2204 and 2406H. A student can earn credit for at most one of 2024 and 2204. A student can earn credit for at most one of 2204 and CMDA 2005.

Prerequisite(s): MATH 1226

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 2204H - Introduction to Multivariable Calculus (3 credits)

Calculus for functions of several variables. Planes and surfaces, continuity, differentiation, chain rule, extreme values, Lagrange multipliers, double and triple integrals and applications, software-based techniques. A student can earn credit for at most one of 2204H and 2406H. A student can earn credit for at most one of 2024 and 2204H. A student can earn credit for at most one of 2024 and 2204H. A student can earn credit for at most one of 2204H and CMDA 2005. **Prerequisite(s):** MATH 1226

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 2214 - Introduction to Differential Equations (3 credits)

Unified course in ordinary differential equations. First-order equations, second-and-higher-order constant coefficient linear equations, systems of first-order linear equations, and numerical methods. Mathematical models describing motion and cooling, predator-prey population models, SIR-models, mechanical vibrations, electric circuits, rates of chemical reactions, radioactive decay. Quantitative and computational thinking to address relevant intercultural and global issues. A student can earn credit for at most one of 2214 and 2406H. A student can earn credit for at most one of 2214 and CMDA 2006.

Prerequisite(s): (MATH 1114 or MATH 2114 or MATH 2114H or MATH 2405H or ISC 2105) and MATH 1226 Pathway Concept Area(s): 5A Quant & Comp Thnk Adv., 11 Intercultural&Global Aware.

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 2214H - Introduction to Differential Equations (3 credits)

Unified course in ordinary differential equations. First-order equations, second-and-higher-order constant coefficient linear equations, systems of first-order linear equations, and numerical methods. Mathematical models describing motion and cooling, predator-prey population models, SIR-models, mechanical vibrations, electric circuits, rates of chemical reactions, radioactive decay. Quantitative and computational thinking to address relevant intercultural and global issues. A student can earn credit for at most one of 2214H and 2406H. A student can earn credit for at most one of 2214H and CMDA 2006

Prerequisite(s): (MATH 1114 or MATH 2114 or MATH 2114H or MATH 2405H or ISC 2105) and MATH 1226

Pathway Concept Area(s): 5A Quant & Comp Thnk Adv., 11 Intercultural&Global Aware.

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 2405H - Mathematics in a Computational Context (5 credits)

Unified course covering topics from linear algebra, differential equations, and calculus for functions of several variables. Comprises the standard second year mathematics courses for science and engineering. 2405H: Vector and matrix algebra, systems of linear equations, linear independence, bases, orthonormal bases, rank, linear transformations and diagonalization. Ordinary linear homogeneous differential equations, implementation with contemporary software. 2406H: Ordinary nonhomogeneous differential equations, calculus for functions of several variables, planes and surfaces, continuity, differentiation, chain rule, extreme values, Lagrange multipliers, double and triple integrals and applications, with software-based techniques. A student can earn credit for at most one of 2114, 2114H, and 2405H. A student can earn credit for at most one of 2204, 2204H, and 2406H.

Prerequisite(s): MATH 1226

Instructional Contact Hours: (5 Lec, 5 Crd)

#### MATH 2406H - Mathematics in a Computational Context (5 credits) Unified course covering topics from linear algebra, differential equations, and calculus for functions of several variables. Comprises the standard second year mathematics courses for science and engineering. 2405H: Vector and matrix algebra, systems of linear equations, linear independence, bases, orthonormal bases, rank, linear transformations and diagonalization. Ordinary linear homogeneous differential equations, implementation with contemporary software. 2406H: Ordinary nonhomogeneous differential equations, calculus for functions of several variables, planes and surfaces, continuity, differentiation, chain rule, extreme values, Lagrange multipliers, double and triple integrals and applications, with software-based techniques. A student can earn credit for at most one of 2114, 2114H, and 2405H. A student can earn credit for at most one of 2204, 2204H, and 2406H. A student can earn credit for at most one of 2214, 2214H, and 2406H.

#### Prerequisite(s): MATH 2405H Instructional Contact Hours: (5 Lec, 5 Crd)

#### MATH 2534 - Introduction to Discrete Mathematics (3 credits)

Emphasis on topics relevant to computer science. Topics include logic, propositional calculus, set theory, relations, functions, mathematical induction, elementary number theory and Boolean algebra. Does not carry credit for mathematics majors, but may be used as though it were a 3000-level elective course for the mathematics minor. Two units of high school algebra, one unit of geometry, one-half unit each of trigonometry and precalculus mathematics required. 2534 may not be taken by math majors for credit without special permission. A student can earn credit for at most one of 2534 and 3034.

Prerequisite(s): CS 1114 or ECE 1574 or ECE 1004 or CS 2064 Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 2644 - Mathematics Tutoring (1 credit)

Introduction to professional, culturally respectful mathematics tutoring. Development of listening and questioning skills, assessment of students' mathematical difficulties. Exploration of teaching and learning processes, effectively utilizing technology, and adjusting instruction to diversity in students' mathematical reasoning. Concurrent mathematics tutoring experience required. May be repeated twice with different leadership expectations for a maximum of 3 credits.

#### Prerequisite(s): MATH 1226

Instructional Contact Hours: (1 Lec, 1 Crd) Repeatability: up to 3 credit hours

# MATH 2964 - Field Study (1-19 credits)

Instructional Contact Hours: Variable credit course

MATH 2974 - Independent Study (1-19 credits) Instructional Contact Hours: Variable credit course

MATH 2974H - Independent Study (1-19 credits) Honors section.

Instructional Contact Hours: Variable credit course

MATH 2984 - Special Study (1-19 credits) Instructional Contact Hours: Variable credit course

MATH 2984H - Special Study (1-19 credits) Instructional Contact Hours: Variable credit course

MATH 2994 - Undergraduate Research (1-19 credits) Instructional Contact Hours: Variable credit course

MATH 2994H - Undergraduate Research (1-19 credits) Instructional Contact Hours: Variable credit course

#### MATH 3034 - Introduction to Proofs (3 credits)

Practice in writing mathematical proofs. Exercises from set theory, number theory, and functions. Propositional logic, set operations, equivalence relations, methods of proof, mathematical induction, the division algorithm and images and pre-images of sets. A student can earn credit for at most one of 2534 and 3034.

Prerequisite(s): MATH 2114 or MATH 2114H or MATH 2405H Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 3124 - Modern Algebra (3 credits)

Introduction to abstract algebraic structures (groups, rings, and fields) and structure-preserving maps (homomorphisms) for these structures. Proof-intensive course illustrating the rigorous development of a mathematical theory from initial axioms.

Prerequisite(s): MATH 3034

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 3134 - Applied Combinatorics and Graph Theory (3 credits)

Emphasis on concepts related to computational theory and formal languages. Includes topics in graph theory such as paths, circuits, and trees. Topics from combinatorics such as permutations, generating functions, and recurrence relations.

Prerequisite(s): MATH 1226 and (MATH 2534 or MATH 3034) Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 3144 - Linear Algebra I (3 credits)

Introductory course in linear algebra. Abstract vector spaces, linear transformations, algorithms for solving systems of linear equations, matrix analysis. This course involves mathematical proofs. **Prerequisite(s):** (MATH 3034 or MATH 2534) and (MATH 2114 or MATH 2114H or MATH 2405H)

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 3214 - Calculus of Several Variables (3 credits)

Fundamental calculus of functions of two or more variables. Implicit function theorem, Taylor expansion, line integrals, Greens theorem, surface integrals.

Prerequisite(s): MATH 2204 or MATH 2204H or MATH 2406H or CMDA 2005

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 3224 - Advanced Calculus (3 credits)

Theory of limits, continuity, differentiation, integration, series. 3224 duplicates 4525.

Prerequisite(s): (MATH 2204 or MATH 2204H or MATH 2406H or CMDA 2005) and MATH 3034

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 3414 - Numerical Methods (3 credits)

Computational methods for numerical solution of non-linear equations, differential equations, approximations, iterations, methods of least squares, and other topics. A grade of C or better required in CS prerequisite 1044 or 1705. A student can earn credit for at most one of 3414 and 4404.

Prerequisite(s): (CS 1044 or CS 1705 or CS 1114 or CS 1124) and MATH 2406H or (CMDA 2005 and CMDA 2006) or (MATH 2214 or MATH 2214H) and (MATH 2204 or MATH 2204H) Instructional Contact Hours: (3 Lec, 3 Crd) Course Crosslist: CS 3414

#### MATH 4044 - History of Mathematics (3 credits)

Historical development of mathematics from antiquity to modern times. Senior standing in mathematics or mathematics education required. **Prerequisite(s):** MATH 3034 **Instructional Contact Hours:** (3 Lec, 3 Crd)

#### MATH 4124 - Introduction to Abstract Algebra (3 credits)

An introduction to the theory of groups and rings. Topics include normal subgroups, permutation groups, Sylows Theorem, Abelian groups, Integral Domains, Ideals, and Polynomial Rings.

Prerequisite(s): MATH 3124 Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4134 - Number Theory (3 credits)

Introduction to elementary number theory. Topics covered may include divisibility, greatest common divisors, unique prime factorization, congruences, Fermat's Little Theorem, Chinese Remainder Theorem, multiplicative number-theoretic functions, Diophantine equations, primitive roots, and the Quadratic Reciprocity Law. **Prerequisite(s):** MATH 3034 or MATH 3134 **Instructional Contact Hours:** (3 Lec, 3 Crd)

#### MATH 4144 - Linear Algebra II (3 credits)

Second course in linear algebra. Similarity invariants, Jordan canonical form, inner product spaces, self-adjoint operators, selected applications. **Prerequisite(s):** MATH 3144

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4175 - Cryptography (3 credits)

4175: Introduction to classical and modern symmetric-key cryptography; alphabetic ciphers, block ciphers and stream ciphers; background in modular arithmetic and probability; perfect secrecy; linear and differential cryptanalysis; Advanced Encryption Standard; hashing. 4176: Introduction to modern public-key cryptography and cryptanalysis; RSA algorithm, ElGamal algorithm, Diffie-Hellman algorithm; digital signatures; background in group theory and number theory; algorithms for primality testing, factoring, and discrete logarithms; elliptic curves.

Prerequisite(s): MATH 3034 or CMDA 3605 or MATH 3134 or MATH 3144 Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4176 - Cryptography (3 credits)

4175: Introduction to classical and modern symmetric-key cryptography; alphabetic ciphers, block ciphers and stream ciphers; background in modular arithmetic and probability; perfect secrecy; linear and differential cryptanalysis; Advanced Encryption Standard; hashing. 4176: Introduction to modern public-key cryptography and cryptanalysis; RSA algorithm, ElGamal algorithm, Diffie-Hellman algorithm; digital signatures; background in group theory and number theory; algorithms for primality testing, factoring, and discrete logarithms; elliptic curves.

Prerequisite(s): MATH 4175 or CMDA 3606 or MATH 3034 or MATH 3134 or MATH 3144

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4225 - Elementary Real Analysis (3 credits)

Real number system, point set theory, limits, continuity, differentiation, integration, infinite series, sequences and series of functions. **Prerequisite(s):** MATH 3224 **Instructional Contact Hours:** (3 Lec, 3 Crd)

#### MATH 4226 - Elementary Real Analysis (3 credits)

Real number system, point set theory, limits, continuity, differentiation, integration, infinite series, sequences and series of functions. **Prerequisite(s):** MATH 4225 **Instructional Contact Hours:** (3 Lec, 3 Crd)

#### MATH 4234 - Elementary Complex Analysis (3 credits)

Analytic functions, complex integration, series representation of analytic functions, residues, conformal mapping, applications **Prerequisite(s):** MATH 3224 **Instructional Contact Hours:** (3 Lec, 3 Crd)

#### MATH 4245 - Intermediate Differential Equations (3 credits)

Solution techniques, linear systems, the matrix exponential, existence theorems, stability, non-linear systems, eigenvalue problems. **Prerequisite(s):** MATH 3224

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4254 - Chaos and Dynamical Systems (3 credits)

Survey of basic concepts in chaotic dynamical systems. Includes material on bifurcation theory, conjugacy, stability, and symbolic dynamics.

Prerequisite(s): (MATH 3034 or MATH 2534) and MATH 3214 Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4324 - Elementary Topology (3 credits)

Basic concepts of topological spaces, continuous functions, connected spaces, compact spaces, and metric spaces.

Prerequisite(s): MATH 3224

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4334 - College Geometry (3 credits)

Transformational approach to Euclidean geometry including an indepth study of isometries and their application to symmetry, geometric constructions, congruence, coordinate geometry, and non-Euclidean geometries.

Prerequisite(s): MATH 3034

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4404 - Applied Numerical Methods (3 credits)

Interpolation and approximation, numerical integration, solution of equations, matrices and eigenvalues, systems of equations, approximate solution of ordinary and partial differential equations. Applications to physical problems. A student can earn credit for at most one of 3414 and 4404.

Prerequisite(s): MATH 4564 and (ESM 2074 or AOE 2074) Instructional Contact Hours: (3 Lec, 3 Crd) Course Crosslist: AOE 4404

#### MATH 4414 - Issues in Scientific Computing (3 credits)

Theory and techniques of modern computational mathematics, computing environments, computational linear algebra, optimization, approximation, parameter identification, finite difference and finite element methods and symbolic computation. Project-oriented course; modeling and analysis of physical systems using state-of-the-art software and packaged subroutines.

Prerequisite(s): (MATH 2214 or MATH 2214H or MATH 2406H or CMDA 2006) and MATH 3214 and (CS 1114 or MATH 1454) Instructional Contact Hours: (2 Lec, 3 Lab, 3 Crd) Course Crosslist: CS 4414

#### MATH 4425 - Fourier Series and Partial Differential Equations (3 credits)

Separation of variables for heat, wave, and potential equations. Fourier expressions. Application to boundary value problems. Bessel functions. Integral transforms and problems on unbounded domains.

Prerequisite(s): MATH 2406H or CMDA 2006 or MATH 2214 or MATH 2214H and MATH 3224

Instructional Contact Hours: (3 Lec, 3 Crd)

MATH 4426 - Fourier Series and Partial Differential Equations (3 credits) Separation of variables for heat, wave, and potential equations. Fourier expressions. Application to boundary value problems. Bessel functions. Integral transforms and problems on unbounded domains.

Prerequisite(s): MATH 4425 Instructional Contact Hours: (3 Lec, 3 Crd)

# MATH 4445 - Introduction to Numerical Analysis (3 credits)

4445: Vector spaces and review of linear algebra, direct and iterative solutions of linear systems of equations, numerical solutions to the algebraic eigenvalue problem, solutions of general non-linear equations and systems of equations. 4446: Interpolation and approximation, numerical integration and differentiation, numerical solutions of ordinary differential equations. Computer programming skills required. **Prerequisite(s):** MATH 2406H or (CMDA 2005 and CMDA 2006) or (MATH 2214 or MATH 2214H) and (MATH 2204 or MATH 2204H) **Instructional Contact Hours:** (3 Lec, 3 Crd)

#### MATH 4446 - Introduction to Numerical Analysis (3 credits)

4445: Vector spaces and review of linear algebra, direct and iterative solutions of linear systems of equations, numerical solutions to the algebraic eigenvalue problem, solutions of general non-linear equations and systems of equations. 4446: Interpolation and approximation, numerical integration and differentiation, numerical solutions of ordinary differential equations. Computer programming skills required. **Prerequisite(s):** MATH 2406H or (CMDA 2005 and CMDA 2006) or (MATH 2214 or MATH 2214H) and (MATH 2204 or MATH 2204H) **Instructional Contact Hours:** (3 Lec, 3 Crd)

#### MATH 4454 - Applied Mathematical Modeling (3 credits)

Analysis of classical and modern applications of mathematics in the physical, biological and social sciences. Emphasis on problem formulating, modeling, solving, simulating, and analyzing results. Programming language required.

Prerequisite(s): MATH 3214

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4564 - Operational Methods for Engineers (3 credits)

Laplace transformations, Fourier series, partial differential equations and separation of variables, boundary value problems, and Sturm-Liouville theory.

Prerequisite(s): (MATH 2214 or MATH 2214H) or MATH 2406H or CMDA 2006

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4574 - Vector and Complex Analysis for Engineers (3 credits)

Vector Analysis: Greens theorem, potential theory, divergence, and Stokes theorem. Complex Analysis: Analyticity, complex integration, Taylor series, residues, conformal mapping, applications. 4574 may not be taken by math majors for credit.

Prerequisite(s): MATH 2204 or MATH 2204H or MATH 2406H or CMDA 2005

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4625 - Mathematics for Secondary Teachers (3 credits)

Course activities will emphasize the curricular themes of problem solving, reasoning and proof, communication, connections, and representation. 4625: Topics in discrete mathematics and algebra from a secondary teaching perspective. 4626: Topics in trigonometry, geometry, measurement, statistics, and probability from a secondary teaching perspective.

Prerequisite(s): MATH 3034 Instructional Contact Hours: (3 Lec, 3 Crd)

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MATH 4626 - Mathematics for Secondary Teachers (3 credits) Course activities will emphasize the curricular themes of problem solving, reasoning and proof, communication, connections, and representation. 4625: Topics in discrete methematics and algebra from a secondary teaching perspective. 4626: Topics in trigonometry, geometry, measurement, statistics, and probability from a secondary teaching perspective.

Prerequisite(s): MATH 3034 Instructional Contact Hours: (3 Lec, 3 Crd)

# MATH 4644 - Secondary School Mathematics With Technology (3 credits)

Use and impact of technology in secondary mathematics curriculum. Various technologies including graphing calculators, calculator based laboratory and probes (CBLs), computer algebra systems, spreadsheets, dynamic geometry software and the Internet will be used to explore secondary mathematical concepts from an advanced viewpoint. **Prereguisite(s):** MATH 3034

Instructional Contact Hours: (3 Lec, 3 Crd)

#### MATH 4664 - Senior Math Education Seminar (2 credits)

A review of basic principles and problem-solving techniques in the eleven topics covered by the Praxis II (Mathematics Content Knowledge) examination. Passing the Praxis II examination prior to student teaching is a state requirement for all students seeking secondary licensure. Passing Praxis I required.

Prerequisite(s): MATH 3124 Instructional Contact Hours: (2 Lec, 2 Crd)

#### MATH 4754 - Internship (1-19 credits)

May be repeated for a maximum of 12 credits. Instructional Contact Hours: Variable credit course Repeatability: up to 12 credit hours

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MATH 4964 - Field Study (1-19 credits)
Instructional Contact Hours: Variable credit course
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MATH 4974 - Independent Study (1-19 credits) Instructional Contact Hours: Variable credit course

MATH 4974H - Independent Study (1-19 credits) Honors section.

Instructional Contact Hours: Variable credit course

MATH 4984 - Special Study (1-19 credits) Instructional Contact Hours: Variable credit course

MATH 4994 - Undergraduate Research (1-19 credits) Instructional Contact Hours: Variable credit course

MATH 4994H - Undergraduate Research (1-19 credits) Honors section.

Instructional Contact Hours: Variable credit course